

Worksheet: Confidence Intervals for Proportions

1. The paralyzed Veterans of America is a philanthropic organization that relies on contributions. They send free mailing labels and greeting cards to potential donors on their list and ask for voluntary contribution. To test a new campaign they recently sent letters to a random sample of 100,000 potential donors and received 4781 donations.

$$E = 1.96 \sqrt{\frac{(0.048)(0.952)}{100000}} = 0.001$$

$$\hat{p} = \frac{4781}{100000} = 0.048 \quad \hat{q} = 0.952$$

- a) Give a 95% confidence interval for the true proportion of those from their entire mailing list who may donate.

$$(0.047, 0.049)$$

- b) A staff member thinks that the true rate is 5%. Given the confidence interval you found, do you find that percentage plausible? Since 5% or .05 is not contained in the 95% conf. interval, I do not think its plausible that the true population proportion is 5%.

2. A national health organization warns that 30% of the middle school students nationwide have been drunk. Concerned, a local health agency randomly and anonymously surveys 110 of the middle 1212 middle school students in its city. Only 21 of them report having been drunk.

$$\hat{p} = \frac{21}{110} = 0.191$$

$$\hat{q} = 0.809$$

- a) What proportion of the sample reported having been drunk?
 b) Does this mean that this city's youth are not drinking as much as the national data would indicate? Not necessarily etc one sample/variability

$$E = 1.96 \sqrt{\frac{(0.191)(0.809)}{110}}$$

- c) Create a 95% confidence interval for the proportion of the city's middle school students who have been drunk.

$$(0.118, 0.263)$$

- d) Is there any reason to believe that the national level of 30% is not true of the middle school students in the city? 30% is outside the interval so yes there is reason to believe the Nat. Av. is wrong

$$E = 0.037$$

- e) To keep the margin of error at most 5%, how many middle school students do we need to survey?

$$n = \hat{p}\hat{q} \left(\frac{z^*}{E}\right)^2$$

$$n = (0.191)(0.809) \left(\frac{1.96}{0.05}\right)^2 = 237.4 \Rightarrow 238 \text{ students}$$

3. In a poll taken in March of 2007, Gallup asked 1006 national adults whether they were baseball fans. 36% said they were. A year previously 37% of a smaller size sample had reported being baseball fans.

$$E = 1.645 \sqrt{\frac{(0.36)(0.64)}{1006}} = 0.025$$

- a) Find the margin of error for the 2007 poll if we want 90% confidence in our estimate of the percent of national adults who are baseball fans.

- b) Explain what the margin of error means. The pop proportion is likely not exactly 36%, so we estimate it will be within a range of values (w/90% conf) within 2.5% of 36%

- c) If we wanted to be 99% confident, would the margin of error be larger or smaller? Bigger

$$E = 2.576 \sqrt{\frac{(0.36)(0.64)}{1006}}$$

$$E = 0.039$$

- d) Find the margin of error for 99% confidence level.

Smaller margins of error correlate to lower conf. levels

- e) In general, all other aspects of the situation remain the same; will smaller margins of error produce greater or less confidence in the interval?
- f) Do you think there's been a change from 2006 to 2007 in the real proportion of national adults who are baseball fans? **No** → 37% is contained in the conf. interval for both 95% + 99%

4. Several factors are involved in the creation of a confidence interval. Among them are the sample size, the level of confidence, and the margin of error. Which statements are true?

- ~~a)~~ For a given sample size, higher confidence means a smaller margin of error. **No**
- b) For a specified confidence level, larger samples provide smaller margins of error. ✓
- c) For a fixed margin of error, larger samples provide a greater confidence.
- ~~d)~~ For a given confidence level, halving the margin of error requires a sample twice as large.
- e) For a given sample size reducing the margin of error will mean lower confidence.
- f) For a certain confidence level, you can get a smaller margin of error by selecting a bigger sample.
- g) For a fixed margin of error, smaller samples will mean lower confidence.
- h) For a given confidence level, a sample 9 times as large will make a margin of error one third as big.